

1) Let  $\sin \theta = \frac{3}{8}$  and  $\sec \theta < 0$ . Find the values of each of the following.

$$y = 3$$

$$r = 8$$

$$x = -\sqrt{55}$$

$$64 = x^2 + 9$$

$$55 = x^2$$

$$\text{A) } \cos \theta = \frac{-\sqrt{55}}{8}$$

$$\text{B) } \csc \theta = \frac{8}{3}$$

2) Simplify by factoring and using fundamental identities to simplify this expression to only one trig function:

$$\sin^2 \theta \cos^2 \theta - \cos^2 \theta$$

$$\begin{aligned} & \cos^2 \theta (\sin^2 \theta - 1) \\ & (\cos^2 \theta)(-\cos^2 \theta) = -\cos^4 \theta \end{aligned}$$

3) **Factor** each expression. Do not use trig identities.

$$\text{A) } \tan^2 \theta - \cos^2 \theta =$$

$$\text{B) } 3 \sin^2 \theta - \sin \theta - 2 =$$

$$\begin{aligned} & \frac{\sin^2 \theta}{\cos^2 \theta} - \cos^2 \theta \\ & (\tan \theta - \cos \theta)(\tan \theta + \cos \theta) \end{aligned}$$

$$(3 \sin \theta + 2)(\sin \theta - 1)$$

4) Use trigonometric substitution to write the algebraic expression as a trigonometric function of  $\theta$ , where  $0 < \theta < \frac{\pi}{2}$ . Use  $x = 5 \sec \theta$

$$\sqrt{4x^2 - 100} =$$

$$\sqrt{4(5 \sec \theta)^2 - 100}$$

$$\sqrt{4(25 \sec^2 \theta) - 100}$$

$$\sqrt{100 \sec^2 \theta - 100}$$

$$\sqrt{100(\sec^2 \theta - 1)} = \sqrt{100 \tan^2 \theta} = 10 \tan \theta$$

5) Verify the identities below algebraically in the vertical format.

$$A) \frac{\sin \theta}{\csc \theta - 1} + \frac{\sin \theta}{\csc \theta + 1} = 2 \tan^2 \theta$$

$$\frac{(\csc \theta + 1) \sin \theta + \sin \theta (\csc \theta - 1)}{\csc^2 \theta - 1}$$

$$\frac{1 + \sin \theta + 1 - \sin \theta}{\cot^2 \theta}$$

$$\frac{2}{\cot^2 \theta} = 2 \left( \frac{1}{\cot^2 \theta} \right) = 2 \tan^2 \theta$$

$$C) (1 + \cot^2 \theta)(1 - \sin^2 \theta) = \cot^2 \theta$$

$$(\csc^2 \theta)(\cos^2 \theta) =$$

$$\left( \frac{1}{\sin^2 \theta} \right) (\cos^2 \theta) =$$

$$\frac{\cos^2 \theta}{\sin^2 \theta} =$$

$$\cot^2 \theta =$$

$$B) \sin^4 \theta \cos^2 \theta - \sin^4 \theta = -\sin^6 \theta$$

$$\sin^4 \theta (\cos^2 \theta - 1) =$$

$$(\sin^4 \theta)(-\sin^2 \theta) =$$

$$-\sin^6 \theta$$

$$D) \frac{1 - \cos^2 \theta}{\cos^2 \theta} = \tan^2 \theta$$

$$\frac{\sin^2 \theta}{\cos^2 \theta} =$$

$$\tan^2 \theta =$$

Solve each trig equation.

$$6) 3 \tan^2 \theta = 1$$

$$\sqrt{\tan^2 \theta} = \sqrt{\frac{1}{3}}$$

$$\tan \theta = \pm \frac{1}{\sqrt{3}}$$

$$\theta = \frac{\pi}{6} + n\pi$$

$$\theta = \frac{5\pi}{6} + n\pi$$

$$\frac{\sqrt{\quad}}{\sqrt{\quad}}$$

$$7) \tan^2 \theta = \tan \theta$$

$$\tan^2 \theta - \tan \theta = 0$$

$$\tan \theta (\tan \theta - 1) = 0$$

$$\tan \theta = 0 \quad \tan \theta = 1$$

$$\frac{\sqrt{\quad}}{\sqrt{\quad}}$$

$$\theta = n\pi$$

$$\frac{\sqrt{\quad}}{\sqrt{\quad}}$$

$$\theta = \frac{\pi}{4} + n\pi$$

Solve each trig equation.

8)  $2\sin^2\theta - \sin\theta = 1$

$$2\sin^2\theta - \sin\theta - 1 = 0$$

$$(2\sin\theta + 1)(\sin\theta - 1) = 0$$

$$2\sin\theta + 1 = 0$$

$$\sin\theta = -\frac{1}{2}$$

$$\sin\theta = 1$$

$$\theta = \frac{\pi}{2} + 2n\pi$$

$$\theta = \frac{7\pi}{6} + 2n\pi \quad \theta = \frac{11\pi}{6} + 2n\pi$$

10)  $3\cos^2\theta - \cos\theta = 4$

$$3\cos^2\theta - \cos\theta - 4 = 0$$

$$(3\cos\theta - 4)(\cos\theta + 1) = 0$$

$$\cos\theta = \frac{4}{3}$$

$$\cos\theta = -1$$

Not in  
range

$$\theta = \pi + 2n\pi$$

9)  $2\sin\theta + \sqrt{3} = 0$

$$\sin\theta = -\frac{\sqrt{3}}{2}$$

$$\theta = \frac{4\pi}{3} + 2n\pi$$

$$\theta = \frac{5\pi}{3} + 2n\pi$$

Give the values of x in the interval  $[0, 2\pi)$ .

11)  $(\cos\theta + 1)^2 = (\sin\theta)^2$

$$\cos^2\theta + 2\cos\theta + 1 = \sin^2\theta$$

$$\cos^2\theta + 2\cos\theta + 1 = 1 - \cos^2\theta$$

$$2\cos^2\theta + 2\cos\theta = 0$$

$$2\cos\theta(\cos\theta + 1) = 0$$

$$\frac{2\cos\theta}{2} = \frac{0}{2}$$

$$\cos\theta = 0$$

$$\theta = \frac{\pi}{2}, \frac{3\pi}{2}$$

$$\cos\theta + 1 = 0$$

$$\cos\theta = -1$$

$$\theta = \pi$$

12)  $\cos\theta = 2$

Not possible, No solution

b/c 2 is not in  
the range  $[-1, 1]$